

$$\#y'' = \frac{-4}{x}y' - \frac{2}{x^2}y + \frac{2 \ln(x)}{x^2}, \quad y(1) = \frac{1}{2}, \quad y(2) = \ln(2)$$

with(LinearAlgebra) :

N := 9 :

a := 1 :

b := 2 :

alpha := $\frac{1}{2}$:

beta := ln(2) :

h := 'h' :

X := Vector(N, i → a + i·h) :

A := $\frac{1}{h^2}$ · Matrix(N, (i, j) → `if`(i = j, -2, `if`(abs(i - j) = 1, 1, 0)));

p := i → - $\frac{4}{X[i]}$:

P := $\frac{1}{2 \cdot h}$ · Matrix(N, (i, j) → `if`(abs(i - j) = 1, p(i) · (j - i), 0));

q := i → - $\frac{2}{X[i]^2}$:

Q := Matrix(N, (i, j) → `if`(i = j, q(i), 0));

M := A - P - Q;

r := i → $\frac{2 \cdot \ln(X[i])}{X[i]^2}$:

R := Vector(N, (i, j) → r(i)) :

R[1] := R[1] - $\frac{\text{alpha}}{h^2}$ - $\frac{p(1) \cdot \text{alpha}}{2 \cdot h}$:

R[-1] := R[-1] - $\frac{\text{beta}}{h^2}$ + $\frac{p(N) \cdot \text{beta}}{2 \cdot h}$:

R;

h := $\frac{(b - a)}{N + 1}$;

evalf(R);

Y := LinearSolve(evalf(M), evalf(R)) :

Y;

plot1 := plot(X, Y, style = point, color = blue) :

f := x → $\frac{4}{x} - \frac{2}{x^2} + \ln(x) - \frac{3}{2}$:

plot2 := plot(f(x), x = 1 .. 2) :

plots[display](plot1, plot2);

residuals := abs(Y - Vector([seq(evalf(f(X[i])), i = 1 .. N)]));